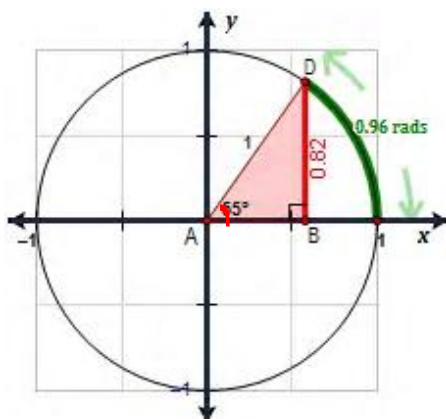
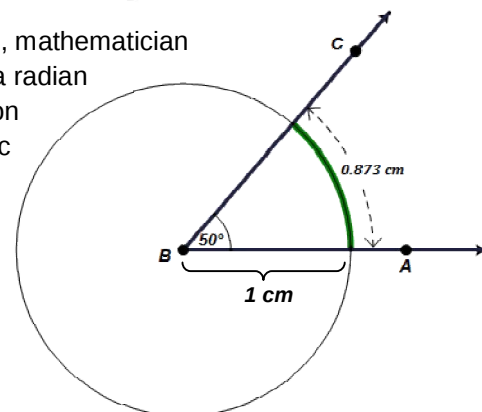


- 1. The Babylonian Degree method of measuring angles.** Around 1500 B.C. the Babylonians are credited with first dividing the circle up in to 360° . They used a base 60 (sexagesimal) system to count (i.e. they had 60 symbols to represent their numbers where as we only have 10 (a centesimal system of 0 through 9)). So, the number 360 was convenient as a multiple of 60. Additionally, according to Otto Neugebauer, an expert on ancient mathematics, there is evidence to support that the division of the circle in to 360 parts may have originated from astronomical events such as the division of the days of a year. So, that the earth moved approximately a degree a day around the sun. However, this would cause problems as years passed to keep the seasons accurately aligned in the calendar as there are 365.242 actual days in a year. Some ancient Persian calendars did actually use 360 days in their year further supporting this idea.



- 2. The transition to Radian measure of angle:** Around 1700 in the United Kingdom, mathematician Roger Cotes saw some advantages in some situations to measuring angles using a radian system. A radian system simply put, drops a unit circle (a circle with a radius of 1) on to an angle such that the center is at the vertex and the length of the intercepted arc is the radian measure. So, a full circle of 360° is equivalent to $2\pi \cdot (1)$ radians. In the example at the right, an angle of 50° is shown. Then, a circle that has a radius of 1 cm is drawn with its center at the vertex. Finally, the intercepted arc length is determined to be approximately 0.873 or more precisely $\frac{5\pi}{18}$ radians.

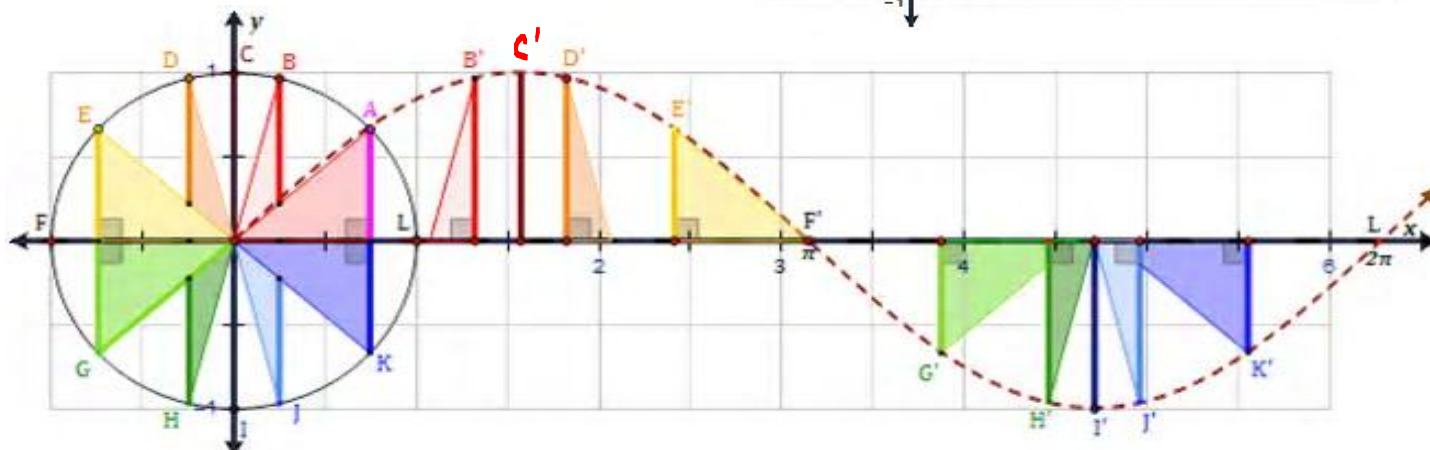
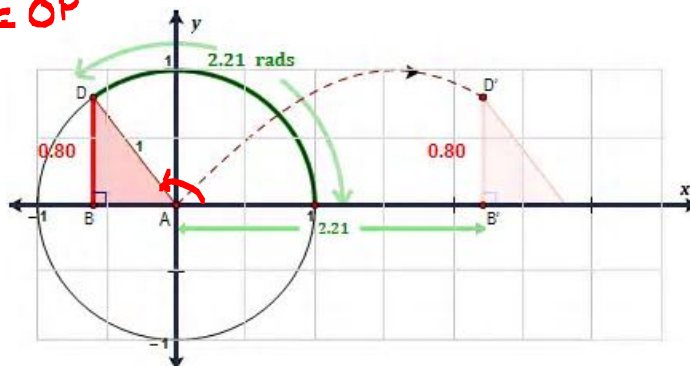


- 3. How Right Triangles create a WAVE:** First consider a right triangle drawn inside of a unit circle like the one shown at the right. Determine the value of $\sin(A)$. Try the example at the right find $\sin(55^\circ)$ which is approximately the same as finding $\sin(0.96 \text{ rads})$.

$$\sin 55 = \frac{\text{op}}{\text{hyp}} = \frac{0.82}{1}$$

$$\sin A = \frac{\text{op}}{1} = \text{op}$$

Then, if we plot each of point where x is the measure of the angle of the unit circle in radians and y is value of $\sin(A)$ which is essentially the height of the right triangle for the given angle. The resulting locus of points generates a Sine Wave. Below shows several right triangles mapping out a sine wave.

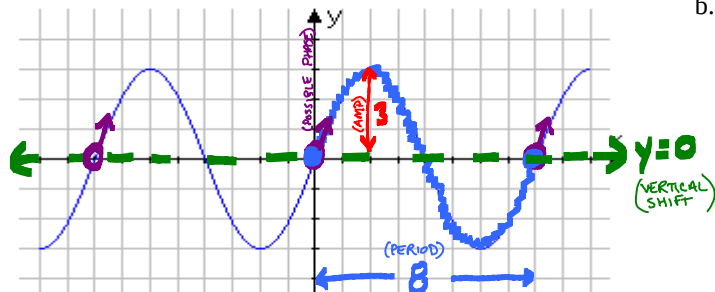


A Sine Wave is commonly described by 4 components.

Parts of a Sine Wave	Visual
Amplitude: The amplitude of a wave is the distance from the midline to highest point of the wave. (half of the vertical displacement). $\text{Amplitude} = \frac{(\text{Highest } Y - \text{Lowest } Y)}{2}$	
Period: The period of the wave is the horizontal distance of one complete cycle. $\text{Period} = (\text{Crest } X) - (\text{Previous Crest } X)$ $\text{Period} = (\text{Trough } X) - (\text{Previous Trough } X)$	
Phase Shift: The amount the wave is shifted right or left $\text{Phase Shift} = \frac{(\text{Crest } X) + (\text{Previous Trough } X)}{2}$	
Vertical Shift: The amount the wave is shifted up or down $\text{Vertical Shift} = \frac{(\text{Highest } Y + \text{Lowest } Y)}{2}$	

1. Find a possible equation of the following graphs.

a.



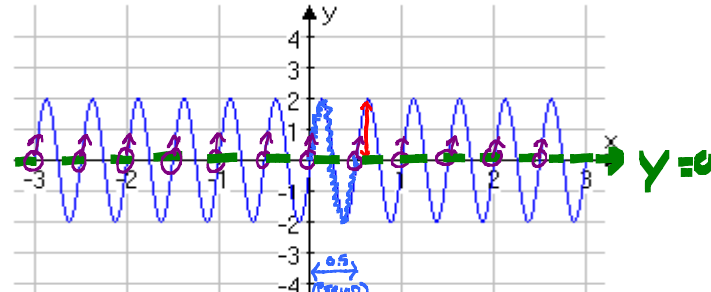
Amplitude = 3

Period = pi

Phase Shift = 0

Vertical Shift = 0

b.



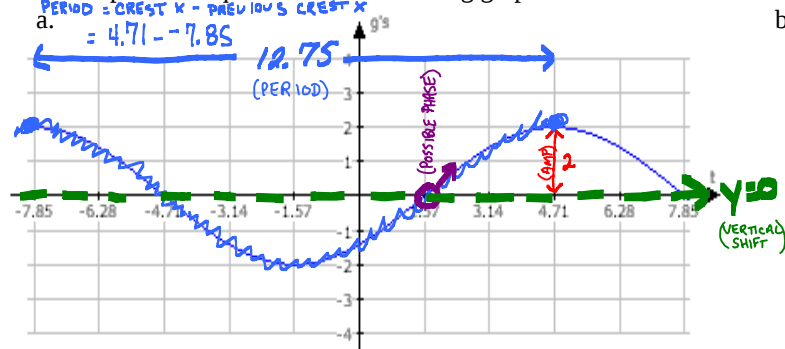
Amplitude = 2

Period = 0.5

Phase Shift = 0

Vertical Shift = 0

2. Find a possible equation of the following graphs.

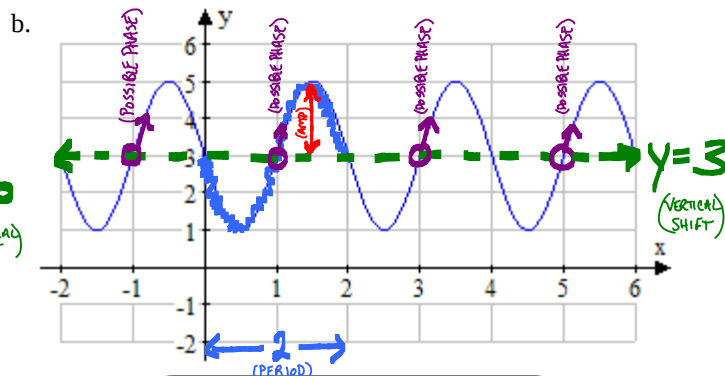


Amplitude = 2

Period = 12.57

Phase Shift = 1.57

Vertical Shift = 0

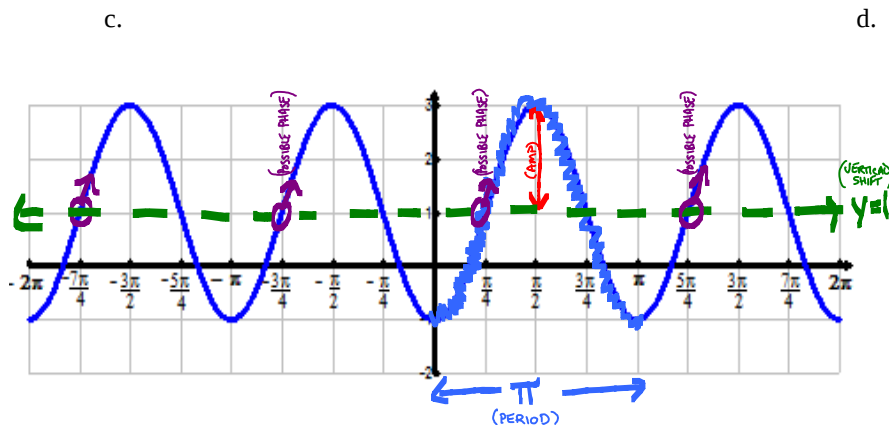


Amplitude = 2

Period = 2

Phase Shift = -1 or 1

Vertical Shift = 3

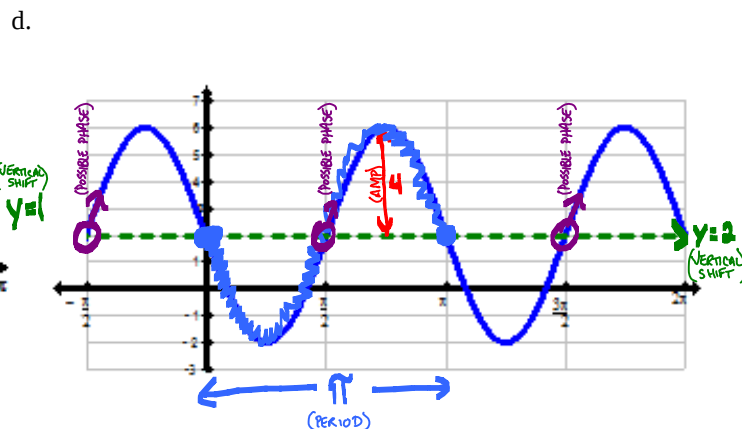


Amplitude = 2

Period = π

Phase Shift = $\frac{\pi}{4}$

Vertical Shift = 1



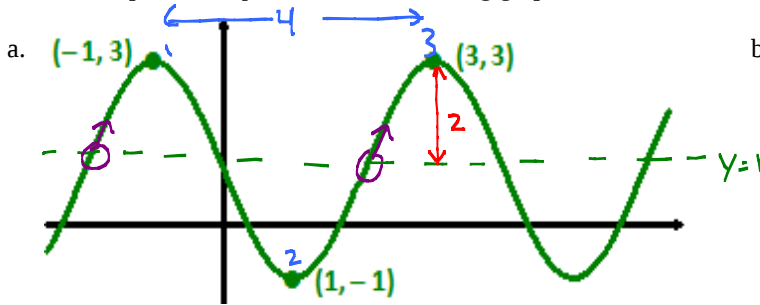
Amplitude = 4

Period = π

Phase Shift = $-\frac{\pi}{2}$ or $\frac{\pi}{2}$

Vertical Shift = 2

3. Find a possible equation of the following graphs.



VERTICAL SHIFT: $\frac{H1Y + LowY}{2} = \frac{3 + (-1)}{2} = \frac{2}{2} = 1$

AMP: $\frac{H1Y - LowY}{2} = \frac{3 - (-1)}{2} = \frac{4}{2} = 2$

PERIOD: $CREST X_3 - CREST X_1 = 3 - (-1) = 4$

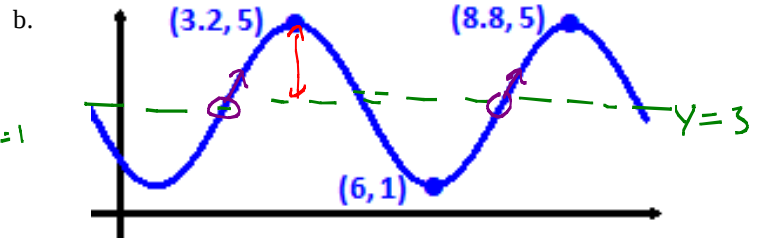
PHASE: $\frac{x_2 + x_3}{2} = \frac{1 + 3}{2} = \frac{4}{2} = 2$

Amplitude = 2

Period = 4

Phase Shift = 2

Vertical Shift = 1



VERTICAL SHIFT: $\frac{H1Y + LowY}{2} = \frac{5 + 1}{2} = \frac{6}{2} = 3$

AMPLITUDE: $\frac{H1Y - LowY}{2} = \frac{5 - 1}{2} = \frac{4}{2} = 2$

PERIOD: $CREST X_3 - CREST X_1 = 8.8 - 3.2 = 5.6$

PHASE: $\frac{x_2 + x_3}{2} = \frac{6 + 8.8}{2} = \frac{14.8}{2} = 7.4$

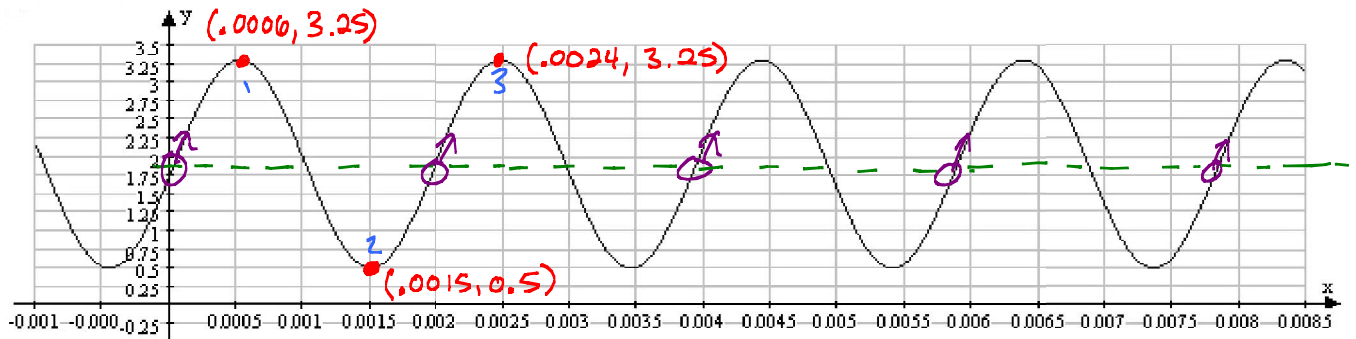
Amplitude = 2

Period = 5.6

Phase Shift = 7.4

Vertical Shift = 3

4. The following is a graph of a tuning fork held up to a CBL microphone.



a. What is the amplitude?

1.375

AMP: $\frac{H1Y - LowY}{2} = \frac{3.25 - 0.5}{2}$

b. What is the Vertical Shift?

1.875

V. SHIFT: $\frac{H1Y + LowY}{2} = \frac{3.25 + 0.5}{2} = \frac{3.75}{2} = 1.875$

c. What is the Period?

.0018

PERIOD: $CREST X_3 - CREST X_1$

$.0024 - .0006 = .0018$

d. What is a possible Phase Shift?

.00195

PHASE: $\frac{x_2 + x_3}{2} = \frac{.0015 + .0024}{2} = \frac{.0039}{2} = .00195$